A Review on Complex System Engineering

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Abstract Complexity is commonly summarized as 'the actions of the whole are more than the sum of the actions of the parts'. Understanding how the coherence emerges from these natural and articial systems provides a radical shift in the process of thought, and brings huge promises for controlling and fostering this emergence. The authors define the term 'Complex System Engineering' to denote this approach, which aims at transferring the radical insights from Complex System Science to the pragmatic world of engineering, especially in the Computing System Engineering domain. A theoretical framework for Complex System Engineering is built by the morphogenetic engineering framework, which identifies a graduation of models, in growing order of generative power. The implementation of Complex System Engineering requires a portfolio of operational solutions: The authors therefore provide a classication of Complex System application approaches to answer this challenge and support the emergence of Complex System Engineers capable of addressing the issues of an ever more connected world.

Keywords Complex networks, complex software engineering, complex systems, design structure matrix, emergent engineering, evolutionary algorithms, organically grown architectures.

1 Introduction

Complexity first denoted the property of objects with many interconnected parts^{[\[1\]](#page-24-0)}. The term is now used to express the behaviour of systems which coherence is drawn from parts interacting locally, such as financial markets, rainforest ecosystems, living organisms, the Internet: Emergence. It is commonly summarized as `the actions of the whole are more than the sum of the actions of the parts'. Understanding how coherence emerges from these natural and artificial systems provides a radical shift in the process of thought, and brings huge promises for controlling and fostering this emergence: In an ever more connected word, being able to control the dynamics of multi-scale systems is a critical skill for success.

However, as stated by Edgar Morin, complexity 'cannot be reduced to a simple idea', it γ cannot be reduced to a law of complexity'^{[\[2\]](#page-24-1)}. It is therefore hopeless to expect the expression

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of simple laws, or a restricted body of knowledge, of complexity. Our research effort in the application of complexity to engineering problems thus draws on the properties of Complex Systems, aims at identifying common methodological patterns, and strive to expose pragmatic solutions both from the scientific literature and in our own contributions.

In this paper, we highlight the research challenges we focus on in this work in Section [2.](#page-1-0) Subsection [2.2](#page-1-1) explicits the way science and engineering interact and complement themselves. Section [3](#page-2-0) presents the main contributions of the field of complex system engineering, and Section [4](#page-7-0) introduces significant applications.

2 Research Challenges

2.1 Engineering and Complex Systems

The field of Complex System Engineering emerges from breakthroughs in the community of morphogenesis^{[\[3\]](#page-24-2)}, embryogenesis^{[\[4\]](#page-24-3)} and artificial life^{[\[5\]](#page-24-4)}, which enable to model and emulate the emergence of heavily interdependent processes such as life. The ability to understand and reproduce these processes provides the basis for building artificial systems with high levels of emergence and interdependencies between their parts.

The research challenge we seek to address is thus:

How to exploit the results of Complex System science for understanding and building arti ficial complex systems?

Our approach is to explicit the different types of complex system models and their application scope to make them actionable for the design of original articial complex systems.

2.2 Engineering and the 'Science of the Artificial'

Since we aim at building artificial complex systems, a pre-requisite for our work is to define engineering as a science. A beautiful definition is given by Herbert Simon in 'The Sciences of the Artificial'^{[\[6\]](#page-24-5)}: A strong distinction is to be made between the Science of the Artificial, i.e., the Science of Engineering and Engineering Sciences. The Science of the Artificial intends to provide a generic analytic framework to investigate articial systems. Engineering sciences define a normative framework for building such systems efficiently.

The research objects of the science of the artificial hold four major characteristics^{[\[6\]](#page-24-5)}:

- 1) Artificial things are synthesized by human being;
- 2) They may imitate appearances of natural ones while lacking the reality of the latter;
- 3) They can be described in term of functions, goals or adaptations;
- 4) They are often discussed in term of imperative as well as descriptive.

Herbert Simon also places a lot of emphasis on the distinction between the Science of the Artificial, which aims at understanding artificial constructs, and the 'Science of Design', i.e., the conception of these 'artificial things'. This 'Science of Design' builds the basis of Engineering science, as the set of natural laws and technical tools necessary to build and operate articial things from the material, mechanical, electronics, computing or engineering domains.

Whereas we aim at transferring knowledge and tools from Complexity Science to Engineering

Science, the discussion on the 'science of the artificial', the object of interest, specific scientific methods, and observed properties of the objects under investigation, build a major aspect for understanding the background of our contributions.

3 The Models of Complex System Engineering

This section illustrates processes for engineering complex systems through three points of view: the architecture, the model, and the process. Architecture design for Complex System engineering is highlighted by the example of research on articial cognition and the quest for reproducing the brain functions^{[\[7,](#page-24-6) [8\]](#page-24-7)}, which emerge from the interconnection of individual neurons. The model types and metrics significant for their evaluation are then detailed^{[\[9,](#page-24-8) [10\]](#page-24-9)}. A classification of processes for building artificial complex systems is presented, using the reference model of organically grown architectures $^{[11]}$ $^{[11]}$ $^{[11]}$.

3.1 Architecture Design and Complex System Engineering: The Brain Model Example

The question of the capability of machines to act like humans was popularized as early as 1950, when Turing published his famous 'imitation game'^{[\[12\]](#page-24-11)} which defines an investigation protocol for evaluating whether a machine can lure a human and make it impossible for him to decide between two interlocutors which one is the human one.

The quest for 'intelligent' machines is pervasive to the history of computer science and expands far beyond the scope of this work. However, the breakthroughs achieved since the 2000's are significant of the challenges of building nature-inspired, artificial systems. Two opposite approaches coexists: The in-silico simulation of natural systems, and the reproduction of system features and properties, with possibly significant deviations or simplifications from the original model. In the case of brain modelling, these two approaches are large brain simulations^{[\[13\]](#page-24-12)}, on the one hand, and biologically inspired cognitive architectures^{[\[14\]](#page-24-13)}, on the other. IBM Blue Brain project is representative of the former^{[\[15\]](#page-24-14)}, and the cat's model of Modha, also from an IBM Team, of the latter^{[\[7\]](#page-24-6)}. The two projects are significantly different: Markram intends to reproduce and understand the behaviour of a real brain, whereas Modha focuses on the brain as organised complexity and on the reproduction of the organ's features. Other projects, such as the CAM-Brain project^{[\[16\]](#page-24-15)} using FPGA technology, deploy a similar feature-oriented approach.

The operational approach of Modha is typical of the approach we explore for designing and building artificial complex systems: Our goal is not to perform breakthrough in natural sciences, but to contribute to the engineering domain. Brain-like architectures typically based on the hypothesis that `the computational building blocks of the brain (neurons and synapses) can be described by relatively compact, functional, phenomenological mathematical models, and that their communication can be summarized in binary, asynchronous messages (spikes)'^{[\[7\]](#page-24-6)}. This approach considers that `the behaviour of the brain apparently emerges via non-random, correlated interactions between individual functional units, a key characteristic of organized complexity. Such complex systems are often more amenable to computer modelling and simulation than to closed-form analysis and often resist piecemeal decomposition'. This strategy is considered in Modha's approach to have brought breakthrough contributions and impressive results.

Another functional model of the brain is the Wang's model^{[\[8\]](#page-24-7)}. Although it provides fewer evaluations of the actual performance of the system, it proposes a complete conceptual framework for cognition. It defines the interactions with the outer world, the buffer, short-term and long-term memory processes, and defines two processing types, the subconscious life function (NI-OS: Natural Intelligence Operating System) and the conscious life functions (NI-App: Natural Intelligence Applications), as depicted in Figure [1.](#page-3-0)

Figure 1 A functional model of the brain^{[\[8\]](#page-24-7)}

Figure [2](#page-4-0) shows the the Layered Reference Model of the Brain $(LRBM)^{[8]}$ $(LRBM)^{[8]}$ $(LRBM)^{[8]}$, which specifies the different, layered functions of natural intelligence at a smaller scale than the functional model: Sensation, memory, perception, action, meta-cognitive functions, and higher cognitive functions.

The challenges of modelling the brain are well representative of the research issues we face in the domain of complex system engineering: The choice between copying the natural interactions or reproducing natural features, the control of emergent interactions between system parts, and multi-layer modelling. It nonetheless introduces a signicant simplication compared to other systems, since a brain model is per denition a centralised system, whereas emergence is also a key property of distributed, heterogeneous systems. We focus here on the macro and architectural challenges, and voluntarily neglect model-internal representations.

Figure 2 The layered reference model of the brain $(LRBM)^{[8]}$ $(LRBM)^{[8]}$ $(LRBM)^{[8]}$

3.2 Modelling Complexity

The second challenge of Complex System engineering is the actual modelling approach used to represent the system and to make it operational. One needs to master the stability of complex engineering systems, and to avoid collapse which may emerge from inadequate optimality $[17]$: In engineering, complexity is often viewed as a source of unsustainability^{[\[18\]](#page-24-17)}. Its sources can be manifold: Design and product development complexity, manufacturing complexity, business and market complexity^{[\[19\]](#page-24-18)}.

Models of complex systems pertain to two families of systems, matching two very different sets of properties: Self Organised Criticality (SOC), and Highly optimized tolerance $(HOT)^{[20]}$ $(HOT)^{[20]}$ $(HOT)^{[20]}$. The properties of Self Organised Criticality characterize systems which are homogeneous, selfsimilar, robust, like algorithms based on artificial ants. Highly Optimized Tolerance (HOT) occurs in structured, heterogeneous, self-dissimilar, robust yet fragile systems^{[\[9,](#page-24-8) [20\]](#page-25-0)}. The brain model is representative of the HOT property.

One important issue while modelling complex systems is the ability to keep the control over the complexity, in particular by tracking the `complexity level' of the system. Very few solutions exist for this: The statistical complexity is one of them. It has been introduced in the context of manufacturing processes. Statistical complexity C_{mu} is defined as the Shannon entropy over the distribution of causal states. $P(S_i)$ denotes the probability of the machine being in state $S_i^{[10]}$ $S_i^{[10]}$ $S_i^{[10]}$:

$$
C_{mu} = \sum_{S_i \in S} P(S_i) * \log_2(P(S_i)).
$$
\n(1)

Statistical complexity C_{mu} is the average amount of historical memory stored in the process, in bits. In a complex process, more information about the past is stored internally either through an explicit memory or through the state of system elements such as their location, speed, etc. Prediction therefore requires more information and is, in turn, more difficult. Further investigation would be required to evaluate the relevance of adapting this metric to more complex processes, as to identify the suitable solutions according to the value of the metric.

Examples of modelling approaches for engineering complex systems are provided in Section [4,](#page-7-0) for illustrating the three representative modelling levels: Network models such as graph and network theory, Collaboration models such as complex adaptative systems and system dynamics, as well as environment model such as stochastic processes.

3.3 Organically Grown Architectures

Although it is currently more geared toward the theoretical evaluation of natural processes, in particular morphogenesis and embryogenesis, the field of Complex System Engineering is actually already defined in the community^{[\[11\]](#page-24-10)}. The processes proposed by Doursat, if they perfectly match artificial life and organically grown architectures, appear to be actually quite well suited for designing operational artificial systems.

The significant contribution of Complex System Engineering as applied to embryogenesis in particular is the focus brought on emergent engineering, i.e., the construction of systems by themselves. This approach provides a radical shift for exploiting controlled self-evolving systems[\[21\]](#page-25-1), and introduces very promising perspectives for engineering processes of technical artefacts, which do not pretend to compete with life processes what regards complexity and emergence levels.

This radical shift also highlights the strong limitations of current engineering approaches:

- Traditional engineering requires a system to be well defined;
- Traditional engineering requires a system's performance to be specified;
- Traditional engineering considers complex systems' emergence as an undesirable 'threat';
- Traditional engineering approaches distributed systems design in a top-down centralised manner.

Emergent engineering, on the contrary, requires to signicantly redene usual target properties of the engineering product and processes (see [\[21\]](#page-25-1) for details):

- Optimality and performance;
- Utility;
- Performance metrics;
- Evolution v.s. evolvability;
- Robustness.

Ideation, design, production, maintenance are thus likely to undergo major mutations under such a paradigm. For instance, embryomorphic engineering supports the creation of decentralized and autonomous systems[\[22\]](#page-25-2). Its application to the generation of swarms such as autonomous robots, or flying or swimming drones, opens broad perspectives.

Complex system engineering approaches are defined as pertaining to four major categories^{[\[11\]](#page-24-10)}, which have originally been elicited for morphogenetic engineering:

- Category I: Constructing (or Assembling, Fitting): A small number of mobile agents or components attach to each other or assemble blocks to build a precise 'stick-figure' structure.
- Category II: Coalescing (or Synchronizing, Swarming): A great number of mobile agents flock and make together dense clusters, whose contours adopt certain shapes.
- Category III: Developing (or Growing, Aggregating): The system expands from a single initial agent or group by division or aggregation, forming biological-like patterns or organisms.
- Category IV: Generating (or Rewriting, Inserting): The system expands by successive transformations of components in the 3D space, based on a grammar of `rewrite' rules.

Figure [3](#page-6-0) shows the design-evolution continuum between engineering and biology: Traditional engineering follows the principle of `intelligent design' (ID), with clearly understood and explicitly defined system architecture and internal models or behaviours. The second step, `intelligent meta-design' (IMD), consist in generative engineering where constraints and target properties are explicit, but the system building is delegated to a machine or an autonomous system. The third step, 'evolutionary meta-design' (EMD), let the system be generated and evolve over generations, while constraints and target properties are still set. The ultimate step, `undesigned evolution' (UE), consists is letting system evolve over generation while no longer using explicit constraint and properties, but exploiting feedback from their environment to lead to an evolutionary `reinforcement learning'.

Figure 3 The design-evolution continuum^{[\[11\]](#page-24-10)}

The field of organically grown architectures thus paves the way towards programmable complex systems, with applications essentially limited to robotics and organ models so $far^[23]$ $far^[23]$ $far^[23]$. Programmable architectures already exist^{[\[24\]](#page-25-4)}. Their patterns for developmental modularity and variability^{[\[25\]](#page-25-5)} build a critical block for their successful implementation.

From intelligent design to undesigned evolution, organically grown architectures open a broad field of endeavour for the nascent field of Complex System engineering, and provides a framework for evaluating the maturity category of complex system approaches: I) Constructing, II) coalescing, III) developing and IV) generating.

4 Applications

In the wide landscape of Complex System tools which can be applied to engineering, three modelling approaches emerge as pragmatic and powerful solutions: Network model (graph and network theory), collaboration model (complex adaptive systems, system dynamics), environment model (stochastic processes). We now illustrate these models through various success stories of Complex System engineering: Risk analysis of utility infrastructure as Complex Networks, risk management in evolving complex manufactured systems such as helicopters through Design Structure Matrices, System Dynamics for understanding accidents, and bio-inspired stochastic computation. We conclude this section by introducing a recent breakthrough in evolutionary engineering: Complex software engineering, which leverages the properties of articial evolution for bringing software quality to the next level.

4.1 Utility Infrastructures as Complex Networks

Complex System have been popularized in the engineering domain by the success of network modelling of utility infrastructures and of their weaknesses. One major contribution in the domain is the work of Gorman^{[\[26\]](#page-25-6)}, who have modelled the US optical fibre network, as well as other critical networks such as the gas network. The theoretical foundations for this research was laid by Barabási under the term 'complex networks'^{[\[27\]](#page-25-7)}.

At the example of the US Internet connections, Gorman illustrates that most physical networks are vulnerable to very localised failures such as a line cut by an excavator, which in the earlier years of Internet already caused major overload in the nationwide network, or to domino effects and major regional blackouts following the shutdown of a single plant on the electrical grid. Figure [4](#page-8-0) shows an example of such a network: The US optical fibre network $^{[26]}$ $^{[26]}$ $^{[26]}$, which scale-free properties make it more efficient, but challenges its robustness. This study also had a major impact towards the awareness of the policy makers with regard to the quantity of information which can be extracted through data available openly, since it was only performed based on non-condential data. It can thus be considered as a key moment in the Open Data movement.

Figure 4 An example of scale-free network: The US optical fiber network^{[\[26\]](#page-25-6)}

Understanding the topology of networks at different scales thus proves to be of core relevance for the analysis of the interconnections of technical or geographical graphs: It help to understand that a dense interconnection does not abolish the distances or ensure per se a great robustness, but that a new set of metrics is needed to characterize, understand, and maintain the networks. These metrics are in particular:

Centrality: The importance of the vertices in a graph and its variations:

Degree centrality: The number of links incident upon a node.

Closeness: Average length of the shortest path between the node and all other nodes.

Betweenness: The number of times a node acts as a bridge along the shortest path between two other nodes.

Clustering coefficient: The degree to which nodes in a graph tend to cluster together.

Diameter: The maximal distance between any pair of its nodes.

Networks are also characterised by their topologies, which can in particular match following models:

random

- Erdós-Rényi (ER) model: With low clustering coefficient and degree distribution converging towards a Poisson distribution[\[28\]](#page-25-8) ,
- Watts-Strogatz model: With small-world properties such as short average path lengths and high clustering^{[\[29\]](#page-25-9)},
- Barabási-Albert (BA) model: With scale-free properties such as power-law degree distributions leading to the presence of hub, with unusually high degree of connectivity with other nodes[\[30\]](#page-25-10) .

Figure [5](#page-9-0) introduces a summary of the difference between random and scale-free networks $^{[27]}$ $^{[27]}$ $^{[27]}$. Figure [6](#page-9-1) illustrates the robustness of a network when facing node removal and Figure [7](#page-9-2) the typical topologies of complex networks^{[\[31\]](#page-25-11)}: Random, small-world and regular.

Figure 5 Random and scale-free networks^{[\[27\]](#page-25-7)}

Figure 6 Robustness of a network when facing node removal^{[\[31\]](#page-25-11)}

Figure 7 Topologies of complex networks $^{[31]}$ $^{[31]}$ $^{[31]}$

Similar approaches have been applied to the study of interdependencies in financial networks $^{[32]},$ $^{[32]},$ $^{[32]},$ as well as subsequent crisis: Knowing the single points of failure, the propagation effects, the

probability of occurrence of given events in multi-scale networks is necessary for efficiently ensuring their robustness. Complex networks certainly constitute the better known tool of complex systems outside the Complex System Science community.

4.2 Keeping the Control over Structural Complexity

Another domain where complexity poses a major practical challenge is the manufacturing of highly technological products, where numerous mechanical and electronic parts interact. In this context, the product behaviour itself does not necessarily show emergent properties, but its de-velopment time^{[\[33\]](#page-25-13)}, reliability^{[\[34\]](#page-25-14)}, design^{[\[35\]](#page-25-15)} as well as its robustness to change propagation^{[\[36,](#page-25-16) [37\]](#page-25-17)} exhibit a high coupling behaviour. The main drivers of complexity in manufacturing are product enablers, process enablers, market forces and social and environmental pressure, as shown in Figure [8.](#page-10-0) Product enablers are the manufacturing technology, the product structure, the control system and software, the product complexity and the customer requirements. Process enablers are the global supply chain, human cognitive ergonomics, planning and scheduling, manufacturing system responsiveness and design tools and methodologies. Market forces imply complexity through global competition, turbulence, variety, short delivery and zero defect objectives, among others. Social and environmental pressure mainly comes from standards and government legislation.

So as to solve these challenges, Design Structure Matrix[∗](#page-10-1) (DSM)[\[38,](#page-25-18) [39\]](#page-25-19) have been proposed, and have evolved since their inception as a research object of their own. Design Structure Matrices represent the dependencies between individual components of systems, which can be interactions based on spatial adjacency, energy flow exchange, information flow exchange or material exchange^{[\[38\]](#page-25-18)}. They can treat both structural dependencies^[38] and time-based dependencies^{[\[33\]](#page-25-13)} and reflect their propagation through several dependency levels.

Figure 8 The drivers of manufacturing complexity

The process of generation of the DSM of a given system[\[40\]](#page-25-20) entails three steps: 1) The creation of the spaghetti graph of the system to be analysed, 2) the extraction of the base

[∗]http://www.dsmweb.org/.

DSM out of this spaghetti graph, and 3) the reordering of this DSM. Reordering aims either at simplification or at identification of significant subsystems. Figure [9](#page-11-0) shows the spaghetti graph for an example system. Figure [10](#page-11-1) shows the base DSM for the example. Figure [11](#page-11-2) shows the related partitioned DSM. The reordering of the DSM underlines the presence of three different types of system component relationships: 1) Parallel $-$ Two components have dependencies to and from the same third parties components, but not between themselves; 2) Sequential One component depends on one another; and 3) coupled — Two components depend on each $\rm\sigma then^{[33]}.$ $\rm\sigma then^{[33]}.$ $\rm\sigma then^{[33]}.$

Figure 9 Step 1 of DSM generation: Spaghetti graph^{[\[40\]](#page-25-20)}

Figure 10 Step 2 of DSM generation: Base DSM[\[40\]](#page-25-20)

Figure 11 Step 3 of DSM generation: Partitioned $DSM^{[40]}$ $DSM^{[40]}$ $DSM^{[40]}$

The four operations which can be applied to DSMs for reordering are the following ones^{[\[40\]](#page-25-20)}:

Partitioning: Manipulating the DSM rows and columns such that the new DSM arrangement does not contain any feedback marks, thus, transforming the DSM into a lower triangular form.

- Tearing: The process of choosing the set of feedback marks that if removed from the matrix (and then the matrix is re-partitioned) will render the matrix lower triangular.
- Banding: The addition of alternating light and dark bands to a DSM to show independent (i.e., parallel or concurrent) activities or system elements.
- Clustering: Finding subsets of DSM elements (i.e., clusters or modules) that are mutually exclusive or minimally interacting^{[\[38\]](#page-25-18)}.

Domain Structure Matrices have been extended to support the heterogeneity of products and processes: Domain mapping matrices^{[\[41\]](#page-25-21)} support the mapping between two domains, for instance tasks and persons, and multiple domain matrices^{[\[42\]](#page-26-0)} enable the analysis of multiple domains having multiple elements.

When composite properties build the subject of analysis, Design Structure Matrices can be combined^{[\[34\]](#page-25-14)}: For instance, risks analysis is performed through the combination of probability and impact matrices. Figure [12](#page-12-0) shows the GKN Westland Helicopters EH101, which evolution is taken as a case study for the evaluation of DSMs as a change propagation management tool. Figure [13](#page-12-1) shows an excerpt of the DSMs used for the risk evaluation of this change management process: Combined likelihood and combined impact of changes in complex manufactured products enable the computation of combined risks of the planned changes. Each technical interdependency inside the system is identified; the probability of propagation of a flaw from any given component to the next is quantified, as well as the importance of the impact of such a flaw. Recursivity then enables to measure the indirect risks of flow propagation from a given component to a remote one inside the target system.

Figure 12 The GKN westland helicopters $EH101^{[34]}$ $EH101^{[34]}$ $EH101^{[34]}$

Figure 13 Use of a design structure matrix for change propagation management^{[\[34\]](#page-25-14)}

4.3 Understanding Accidents

The analysis of emergent properties of complex artificial or natural environments is the subject of the System Dynamics^{[\[43\]](#page-26-1)} field. In System Dynamics, ecosystems or organisations are modelled through the positive of negative feedback its elements $-$ Or rather its key indicators — Exercise over each other. Accident analysis is a field which is well understood. The STAMP: Systems-Theoretic Accident modelling and Processes^{[\[44\]](#page-26-2)} provides a comprehensive illustration of the capability of this approach. Its goal is resilience in safety-critical systems[\[45\]](#page-26-3). It is based on three core concepts: Constraints, hierarchical levels of control, and process models. It emphasizes the distinction between development and operations. STAMP is based on the risk management framework by Rasmussen^{[\[46\]](#page-26-4)} which takes hazard source characteristics as well as the full socio-technical system and environmental stressors into account for the analysis: Government, regulators and associations, companies, management, staff and work.

The models of System Dynamic are built by three main types of feedback loops between their elements: The reinforcing loop, shown in Figure [14,](#page-13-0) the balancing loop, shown in Figure [15,](#page-13-1) and the balancing loop with a delay, shown in Figure $16^{[47]}$ $16^{[47]}$ $16^{[47]}$. The models can be one-scale model, where individual metrics interact with one another, and multi-scale models, where submodels interact with one another. Tools like $VENSIM^{\dagger}$ or others support the approach.

Figure 14 System dynamics: Reinforcing $loop^{[47]}$ $loop^{[47]}$ $loop^{[47]}$

Figure 16 System dynamics: Balancing loop with a delay^{[\[47\]](#page-26-5)}

Figure [17](#page-14-0) shows an excerpt of the model for the multi-scale risk management analysis of Shuttle Columbia loss, performed at $NASA^{[48]}$ $NASA^{[48]}$ $NASA^{[48]}$. Considered risk submodels are launch rate, perceived success by the administration, system safety resource allocation, shuttle ageing and maintenance, system safety knowledge, skills and staffing, incident learning and corrective ac-

[†]http://vensim.com/.

tion, as well as system safety effort and efficacy. The risk level, which quantification is the target of this investigation, is a model variable for itself.

Figure 17 The multi-scale risk management analysis of Shuttle Columbia $loss^{[48]}$ $loss^{[48]}$ $loss^{[48]}$

The modelling using System Dynamics for real-world systems is performed in six steps^{[\[43\]](#page-26-1)}. This integrated approach from analysis to deployment implies a very thorough validation of field tests and data on which the conclusion are drawn $^{[49]}$ $^{[49]}$ $^{[49]}$.

- Description of the system;
- Conversion of the description to level and rate equations;
- Simulation of the model;
- Design of alternative policies and structures;
- Educate and debate;
- Implement changes in policies and structures.

The evolution of the key indicators over time build the output of the model. They provides significant insights over the behaviour of the system, as well as over potential countermeasures against observed flaws. For instance, Figure [18](#page-14-1) shows perceived priorities w.r.t. performance and safety at NASA during the preparation process of spatial flights^{[\[47\]](#page-26-5)}. Figure [19](#page-15-0) depicts the relative impact of fixing symptoms only v.s. fixing systemic factors.

Figure 18 Perceived priorities: Performance v.s. safety^{[\[47\]](#page-26-5)}

Figure 19 Impact of fixing symptoms only v.s. fixing systemic factors^{[\[47\]](#page-26-5)}

In cases where only indicators are available from the environment under analysis, System Dynamics provides an efficient framework for modelling the retroactive loops between the various system and environment indicators. A thorough evaluation of the model w.r.t. actual system state enables to evaluate hypotheses and deploy them in the wild. It therefore builds another very pragmatic approach for Complex System modelling applied to the engineering of real products or organisations.

4.4 Bio-Inspired Stochastic Computation

In the field of Computer Science, complexity is tightly bound with Complexity Theory and problems causing combinatorial explosion if one searches to find solutions through systematic exploration, like the Traveling Salesman Problem (TSP). These problems typically pertain to the NP-hard problem category, and although they are not recent, require a radical shift w.r.t. other algorithm types. The idea of exploiting evolution in the computing domain is almost as old as the transistor itself — The first computing efforts on evolution date back to $1954^{[50]}$ $1954^{[50]}$ $1954^{[50]}$. The theory of this new insight came in the mid-70's as a bio-inspired, stochastic computation approach: Evolutionary algorithms^{[\[51\]](#page-26-9)}. Actual applications came more than one decade later^{[\[52\]](#page-26-10)}, and the beginning of the XXI's century brought the first significant technological successes of evolutionary approaches, such as the generation of highly focused satellite antennas for the NASA[\[53\]](#page-26-11). This dissemination goes along the creation of complementary bio-inspired, stochastic algorithms, such as Ant-Colony Optimisation (ACO) or Particle Swarm Optimisation (PSO).

Evolutionary Algorithms (EAs)

are bio-inspired algorithms which rely on Darwinian theory of evolution^{[\[54\]](#page-26-12)}. They come in four main flavours^{[\[55\]](#page-26-13)}:

- Genetic algorithms where the solutions are typically represented as strings or binary, and evolve through recombination and mutation^{[\[51,](#page-26-9) [56\]](#page-26-14)}. These algorithms are typically used for optimisation problems^{[\[57\]](#page-26-15)}, machine learning^{[\[58\]](#page-26-16)}, or classifiers^{[\[59\]](#page-26-17)}.
- **Evolution strategies** where the potential solutions are represented by numerical vectors^{[\[60](#page-26-18)–[62\]](#page-26-19)}. The mutation process is in most cases self-adaptive. They have applications in particular for parameter optimisation[\[62,](#page-26-19) [63\]](#page-27-0) .
- Genetic programming considers full-fledged computer programs as the artefacts under mu-tation, rather than individual solutions to formal problems^{[\[64\]](#page-27-1)}. The fitness of the program is evaluation w.r.t. a predefined task.
- Evolutionary programming is similar to Genetic programming, but the program structure itself is fixed, while only its numerical parameters are allowed to evolve^{[\[65,](#page-27-2) [66\]](#page-27-3)}. Often, Finite State Machines are used as predictors.

The individual solutions can thus be either strings, binary, numeric values, parametrized programs, or full-fledge programs. Hybrid approaches are frequent. For instance, so-called memetic algorithms^{[\[67\]](#page-27-4)} combine a population-based genetic algorithm with specific meta-heuristics for local searches. This approach is in particular efficient for multi-objective problem solving. Genetic algorithms can also be combined with differential evolution^{[\[68\]](#page-27-5)} for improving local search^{[\[69\]](#page-27-6)}.

Multi-objective problems are not resolved through a single individual, which would be tter than the others, but through a set of individuals providing a balanced trade-off between the objectives^{[\[70,](#page-27-7) [71\]](#page-27-8)}. This set of better fitting individuals, called 'non-dominated', can be visualised with a so-call Pareto front. Figure [20](#page-16-0) depicts the various topologies of Pareto fronts for multi-objective problems solved using Evolutionary Algorithms. A whole family of dedicated multi-objectives evolutionary algorithms (MOEAs) addresses the extraction of pareto-optimal solutions through evolutionary algorithms: $NSGA2^{[72]}$ $NSGA2^{[72]}$ $NSGA2^{[72]}$, $NSGA3^{[73]}$ $NSGA3^{[73]}$ $NSGA3^{[73]}$, $ASREA^{[74]}$ $ASREA^{[74]}$ $ASREA^{[74]}$, $PAES^{[75]}$ $PAES^{[75]}$ $PAES^{[75]}$ and $ESPEA^[76]$ $ESPEA^[76]$ $ESPEA^[76]$.

Figure 20 The various topologies of Pareto fronts for multi-objective problems solved using Evolutionary Algorithms[\[70\]](#page-27-7)

Figure [21](#page-18-0) shows the generic process for Evolutionary Algorithms^{[\[55,](#page-26-13) [58\]](#page-26-16)}, which is are made up of four main steps:

- Initialisation The population of potential solutions is created, mostly in a random way, as shown in Figure [22.](#page-18-1)
- Evaluation The current population, either the initial population or the evolved population, is evaluated w.r.t. the fitness function. The fitness function is a numerical value which enables to rank the quality of each individual. A better fitness is typically represented through a smaller fitness value. The fitness function of the population is usually bound

with a stop criteria, together with other algorithmic metrics such as the number of iterations: if a sufficiently effective solution is found, or if the search is too long, the algorithm stops and returns the current population as output.

- Selection The individuals which are considered the fitter for serving as basis for the creation of the next generation are kept in the system. Often, the best individuals are kept, but sometimes heterogeneous solutions enable to foster exploration of the search space and reduce the risk of sticking to local optima.
- Evolution Three main strategies for evolution exist:
	- Haploïd reproduction i.e., reproduction from a single cell. It is typically implemented through the mutation operator shown in Figure [23](#page-18-2) and applied to a single parameter of one given candidate solution.
	- N-ploïd reproduction i.e., reproduction from several cells. It supports evolution from several existing candidate solutions, as shown in Figure [24.](#page-18-3) It is for instance typical of Particle Swarm Optimisation (PSO)^{[\[77\]](#page-27-14)}.
	- Sexual reproduction typically from two cells. It relies on two individuals to create a third one which pertains to the new generation, through the mutation and cross-over operators, as shown in Figure [25.](#page-19-0)

The two principal operators for evolution are:

- Mutation that consists in altering the value of one single individual. It can be performed at random, near the current value, as in Particle Swarm Optimisation (PSO)[\[77\]](#page-27-14) or Harmony search strategy^{[\[78\]](#page-27-15)}, or consider values of solutions with better evaluation, as in differential evolution^{[\[68\]](#page-27-5)}.
- Cross-over that consists in the exchange of one or several parameters (the `chromosomes') between a pair of individuals of the potential solution set.

Throughout the evolutionary computation process, the evolution step is performed in two phases:

- Exploration during the first iterations, consists in generating candidate solutions over the whole search space, as shown in Figure [26.](#page-19-1)
- Exploitation during later iterations, consists in generating candidate solutions based on efficient existing solutions to perform local search, as shown in Figure [27.](#page-19-2)

Figure 21 The generic process for Evolutionary Algorithms

Figure 22 Evolutionary algorithms: The initialisation step

Figure 23 Evolutionary algorithms: The haploïd reproduction strategy for the evolution step

Figure 24 Evolutionary algorithms: The N-ploïde reproduction strategy for the evolution step

Figure 25 Evolutionary algorithms: The sexual reproduction strategy for the evolution step

Figure 26 Evolutionary algorithms: The exploration phase of the evolution step

Figure 27 Evolutionary algorithms: The exploitation phase of the evolution step

Each particular Evolutionary Algorithm uses a combination of this overall process^{[\[79\]](#page-27-16)}. The status of the population being evolved can be of two types: In the Pittsburgh-strategy for Evolutionary Algorithms[\[80\]](#page-27-17), the population is built of individual candidates, and the problem solution is built out of a single individual of the population, as shown in Figure [28;](#page-20-0) in the Parisian-strategy for Evolutionary Algorithms, the population is built of partial candidates, and the problem solution is built out of several individuals of the population, as shown in Fig-ure [29.](#page-20-1) This distinction is in particular exploited in Learning Classifier Systems (LCS)^{[\[55,](#page-26-13) [81\]](#page-28-0)}. Pittsburgh-LCS^{[\[80,](#page-27-17) [82,](#page-28-1) [83\]](#page-28-2)} defines a population of classifier-sets, the problem solution is built out

of one individual of the population. Michigan-LCS^{[\[79,](#page-27-16) [84,](#page-28-3) [85\]](#page-28-4)} define a population built of individual classifiers, and the problem solution is built out of several individuals of the population. The Parisian approach^{[\[86\]](#page-28-5)} consists in the generalisation of the Michigan approach to generic Evolutionary Algorithms^{[\[87\]](#page-28-6)}. It has been in particular evaluated for Iterated Function Systems (IFS), which build systems of functions for generating fractals.

Figure 28 Evolutionary algorithms: Pittsburgh-strategy in the selection step

Figure 29 Evolutionary algorithms: Parisian-strategy for the selection step

The efficiency of Evolutionary Algorithm depends on the balance between the phases of exploration, where the overall landscape is discovered, and exploitation, where local search is performed^{[\[88\]](#page-28-7)}. This balance can be improved by the island model, where local islands exchange individuals from time to time to reduce the risk of being trapped in local optima^{[\[89,](#page-28-8) [90\]](#page-28-9)}. The island model provides a theoretical basis for distribution of EAs, either on CPU^{[\[91\]](#page-28-10)} or on General Purpose Graphical Programming Units (GPGPU)^{[\[92\]](#page-28-11)}. Such architectures exhibit interesting properties such as the capacity to obtain supralinear performance w.r.t. the actual processing power[\[93\]](#page-28-12) .

4.4.1 Alternative Stochastic Algorithms

In order to exploit bio-inspired stochastic computing in domains where evolutionary algorithms do not outperform, several complementary approaches have been developed. One of the most famous is Ant-Colony Optimisation $(ACO)^{[94]}$ $(ACO)^{[94]}$ $(ACO)^{[94]}$, which are based on work on the Ar-gentina ant 'Iridomyrnex Humilis' by Deneubourg^{[\[95,](#page-28-14) [96\]](#page-28-15)}. Whereas EAs intend to solve complex problems through a population based approach, ACOs exploit the emergent properties of collaborating unitary agents, which interactions enable to identify efficient paths in dynamic envi-ronments through the deposit of pheromones: This is stygmergy. Figure [30](#page-21-0) shows 'Iridomyrnex Humilis' ants finding a short path through two bridges between nest and food^{[\[97\]](#page-28-16)}. Photos are shot 4 and 8 minutes after the bridge is set, respectively.

Other approaches are Particle Swarm Optimisation $(PSO)^{[77]}$ $(PSO)^{[77]}$ $(PSO)^{[77]}$ for local search strategies, Harmony Search which combines a genetic algorithm with a local search strategy^{[\[78\]](#page-27-15)}, or the Fly algorithm^{[\[98\]](#page-28-17)} for identifying moving objects in video processing. The exhaustive presentation of these algorithms goes far beyond the scope of this contribution. We will therefore not elaborate further on them. As a conclusion, bio-inspired stochastic algorithms introduce non-deterministic optimisation for complex problems, and provides mutation and cross-over mechanisms able to solve complex problems as well as to generate original knowledge. They therefore lay a solid basis for studying complex problems in the Computer Science field.

Figure 30 'Iridomyrnex Humilis' ant finding a short path through two bridges between nest and $food^[97]$ $food^[97]$ $food^[97]$

4.5 Complex Software Engineering

One of the most recent breakthroughs in the application of Complex System science to engineering is the Genetic Improvement (GI) of programs^{[\[99\]](#page-28-18)}, originally known as Probabilistic incremental program evolution (PIPE)^{[\[100\]](#page-28-19)}. This approach is a major milestone towards the automation of programming, and thus opens great perspectives for the evolution of the job of software developers.

Genetic Improvement is defined as the process of using computational search techniques to improve existing software in particular in terms of correctness (bug fixing), execution time, or power consumption^{[\[101\]](#page-29-1)}. It consists in the automated evolution of software programs, under the form of code, abstract code representation, or even binary packages. One of the key findings of GI is that, unintuitively, software is very robust to mutations: In a reference experiment,

Langdon shows that more than 60 % of the mutations of a given test program have actually no impact on the behaviour of the program whatsoever^{[\[102\]](#page-29-2)}. Figure [31](#page-22-0) illustrates the results of this experiment on random changes in code lines: 4400 out of 7079 mutations, on the StereoCamera kernel on an NVidia GeForce FT 730 graphic card, i.e., 62%, have not impact on the execution. 41 mutations, i.e., 0,58%, of the mutations conserve the program functionalities while actually improving its performances. Other 38 % of mutations negatively alter functionality or performance.

Fig. 2. Impact of all (7079) one change mutations on StereoCamera kernel [16] ng on an nVidia GeForce GT 730 graphics card. Nine mutants failed to compile due to a bug in the nVidia CUDA 6.0.1 compiler (fixed in CUDA 7.0). compare are or a bug in the invariant cluster failed at run-time. 4400 (62%) mutants do not
thange the output at all ("no change"), indeed at least 41 of them are faster (x) .

Figure 31 The impact of random changes in code lines^{[\[102\]](#page-29-2)}

One of the operational challenge for such approaches is of course that the test cases, which serve as reference for the evaluation of the fitness function of the program, must cover all explicit as well as implicit requirements of the software: Otherwise, new bugs or inconsistencies can appear unnoticed. A complete coverage is far from being achieved in most software projects so far, so the application of Genetic Improvement implies a radical shift in the quality of the software engineering process.

GenProg[\[103\]](#page-29-3) is one of the reference framework for Genetic Improvement. It proved capable of solving bugs which are very tedious to correct manually, such as segmentation faults, for programs of length of several millions lines of code. GenProg represents a program as a pair of:

- An abstract syntax tree (AST) that includes all of the statements in the program;
- A weighted path consisting of a list of program statements, each associated with a weight based on that statement's occurrence in the execution traces of various test cases.

The update operator of the genetic algorithm alters the path. This alteration is reflected back in the program AST. The process iterates until the fitness function confirms that the test cases execute without error. The potential drawbacks of this approach are usually more than compensated by the rapid generation of robust software patches, but need nonetheless to be taken into account: High costs are bound with repairs that actually degrade the functionality, in case of insufficient code coverage by tests, or with the application of repairs following false positives generated by intrusion detection systems, i.e., which actually do not match an actual vulnerability or instability in the program.

The issue of code coverage poses a major challenge for the wide dissemination of GI. Therefore, some authors propose an iterative process including regular interactions with the user, so as to complete the test case set: Figure [32](#page-23-0) shows a three-stage evolutionary approach for evo-lutionary software repair by Schulte^{[\[104\]](#page-29-4)}, applied to firmware and drivers. The exploitation of the expert feedback also enables a radical shift in the type of programs which can be corrected: rather than considering the program code only, or an abstract representation of the code as AST, it becomes possible to repair program binaries, with little to no preliminary knowledge about the program. First, the vulnerable executable binary is extracted from the firmware. Next, the program is mutated in order to find versions of the executable which solves the bugs or vulnerabilities. Then, the user interactively adds test cases that covers the functionalities broken by the current mutation. The process iterates until an actual program repair is found.

Figure 32 An approach for evolutionary software repair^{[\[102\]](#page-29-2)}

Fine-tuning the Genetic Improvement process requires to define specific metrics for the underlying genetic algorithms^{[\[101\]](#page-29-1)}: The fitness functions is specific to the objective of the GI process, and needs to take into account the evaluation of the functional stability of the program. For bug fixing it is inherently discrete, whereas it becomes continuous when the objective is to improve execution time or to reduce memory consumption. The edit distance measures the number of mutations between two valid programs, and thus evaluates the depth of the performed alterations.

Genetic Improvement paves the way to program synthesis: For instance, evolutionary soft-ware sketching^{[\[105\]](#page-29-5)} enables to quicken the generation of full programs by the machine: Instead of generating a comprehensive program, a first sketch is created by the developers, and serves as basis for the synthesis of missing parts. This approach provides competitive performances w.r.t. full synthesis. The proposed approach lays on Satisfiability Modulo Theories $(SMT)^{[106, 107]}$ $(SMT)^{[106, 107]}$ $(SMT)^{[106, 107]}$ $(SMT)^{[106, 107]}$, a form of the constraint satisfaction problem.

5 Conclusions and Perspectives

Complex System approaches, in particular Evolutionary Algorithms, provide a very promising way to explore the search space of highly complex artefacts like software programs. They are likely to take even more significance as the fields of Genetics Improvement, meant for program optimisation and repair, and Program Synthesis, which aims at generating full applications, will gain in maturity. These evolutions will highly probably bring major disruption in the IT and development industry, and job market, in the coming decades.

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